

# Aluminum Oxide Nanoparticle Films Deposited from a Nonthermal Plasma: Synthesis, Characterization, and Crystallization

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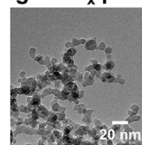
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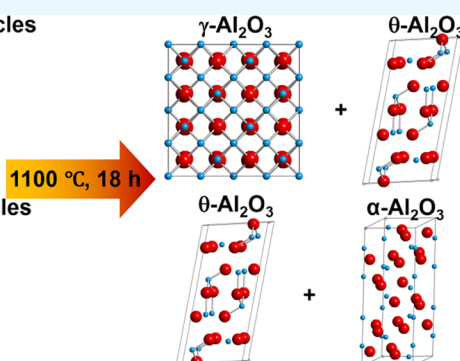
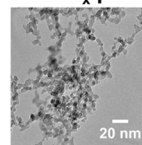
Supporting Information

**ABSTRACT:** Aluminum oxide, both in amorphous and crystalline forms, is a widely used inorganic ceramic material because of its chemical and structural properties. In this work, we synthesized amorphous aluminum oxide nanoparticles using a capacitively coupled nonthermal plasma utilizing trimethylaluminum and oxygen as precursors and studied their crystallization and phase transformation behavior through postsynthetic annealing. The use of two reactor geometries resulted in amorphous aluminum oxide nanoparticles with similar compositions but different sizes. Size tuning of these nanoparticles was achieved by varying the reactor pressure to produce amorphous aluminum oxide nanoparticles ranging from 6 to 22 nm. During postsynthetic annealing, powder samples of amorphous nanoparticles began to crystallize at 800 °C, forming crystalline  $\theta$  and  $\gamma$  phase alumina. Their phase transformation behavior was found to be size-dependent in that powders of small 6 nm amorphous particles transformed to form phase-pure  $\alpha$ - $\text{Al}_2\text{O}_3$  at 1100 °C, while powders of large 11 nm particles remained in the  $\theta$  and  $\gamma$  phases. This phenomenon is attributed to the fast rate of densification and neck formation in small amorphous aluminum oxide particles.

large  $\text{AlO}_x$  particles



small  $\text{AlO}_x$  particles



## 1. INTRODUCTION

Aluminum oxide ( $\text{Al}_2\text{O}_3$ ), commonly known as alumina, is one of the most widely used inorganic ceramic materials because of its superior thermal, chemical, and structural properties. Alumina can exist in both amorphous and crystalline forms. Amorphous alumina is considered to be an excellent candidate for anodic materials, gate insulators in transistors, protective coatings, and catalysts.<sup>1–5</sup> Various methods have been employed to synthesize amorphous alumina nanoparticles, which include sol–gel processing,<sup>6,7</sup> solution combustion,<sup>8–12</sup> precipitation,<sup>13–15</sup> ultrasonic treatment of porous anodic alumina membranes,<sup>16</sup> energetic pulsed laser ablation,<sup>17</sup> and tragacanth gel synthesis.<sup>18</sup>

The structure of amorphous alumina has been studied extensively and found to be comprised of a network of  $\text{AlO}_4$  tetrahedra,  $\text{AlO}_5$  polyhedra, and small fractions of  $\text{AlO}_6$  octahedra.<sup>19–24</sup> Solid-state  $^{27}\text{Al}$  nuclear magnetic resonance studies revealed that the existence of a significant fraction of  $\text{AlO}_5$  polyhedra, where  $\text{Al}^{3+}$  ions are penta-coordinated with oxygen ions, creates disorder and hinders the crystallization and growth of crystalline alumina phases.<sup>25</sup> Thus, high temperatures ( $\sim 800$  °C) are required for the transformation of amorphous to crystalline alumina nanoparticles.<sup>26</sup> This process involves a structural rearrangement reaction converting  $\text{AlO}_5$  polyhedra into  $\text{AlO}_4$  and  $\text{AlO}_6$ .

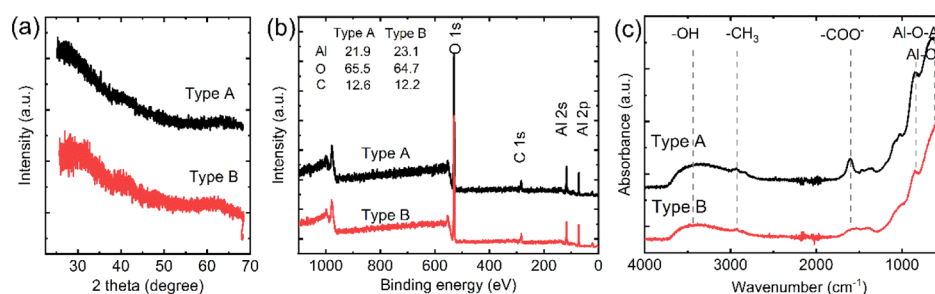
Phase transformation of amorphous to crystalline alumina nanoparticles can greatly depend on several parameters such as the synthetic route, heating rate, grain size, and chemical composition. Crystalline alumina can exist in various metastable crystalline phases ( $\chi$ ,  $\eta$ ,  $\delta$ ,  $\kappa$ ,  $\theta$ ,  $\gamma$ , and  $\rho$ )<sup>27–29</sup> and corundum, or  $\alpha$ -alumina is identified as the most thermodynamically stable phase in bulk form. The typical phase transformation sequence in crystalline alumina can be depicted as  $\gamma \rightarrow \delta \rightarrow \theta \rightarrow \alpha$ - $\text{Al}_2\text{O}_3$ .<sup>26</sup> The transformation of  $\gamma$ - $\text{Al}_2\text{O}_3$  (density  $\rho = 3.56$  g cm<sup>−3</sup>) to  $\alpha$ - $\text{Al}_2\text{O}_3$  ( $\rho = 3.98$  g cm<sup>−3</sup>) is accompanied by a volume reduction of about 10% and proceeds through a meta-phase of  $\theta$ - $\text{Al}_2\text{O}_3$ .<sup>30</sup> Typically, the final transformation to  $\alpha$ - $\text{Al}_2\text{O}_3$  requires higher annealing temperature around 1100 °C.<sup>26</sup> With superior hardness, low friction, unique heat-transfer properties, and excellent wear resistance,  $\alpha$ - $\text{Al}_2\text{O}_3$  plays a critical role in the production of advanced ceramic materials and as a core and filler material for nanocomposites.<sup>31–33</sup>  $\gamma$ - $\text{Al}_2\text{O}_3$  nanoparticles themselves also

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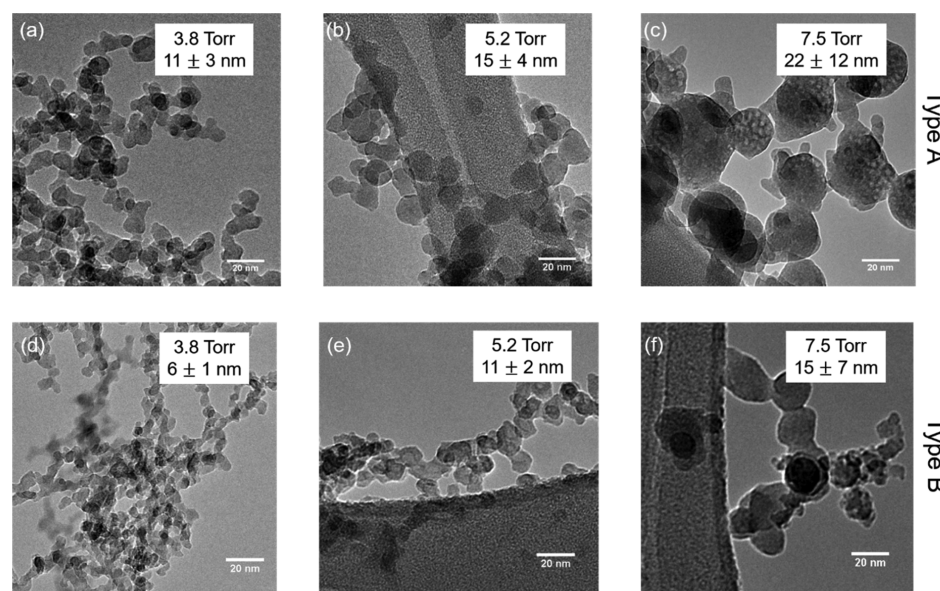
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**Figure 1.** Characterization of  $\text{AlO}_x$  nanoparticles synthesized from type A and type B reactors at  $p = 3.8$  Torr: (a)  $\theta$ – $2\theta$  mode out-of-plane XRD patterns of the as-synthesized  $\text{AlO}_x$  nanoparticles from type A and type B reactors. (b) XPS survey scan of  $\text{AlO}_x$  nanoparticles from type A and type B reactors. (c) Typical FTIR spectra of  $\text{AlO}_x$  samples from type A and type B reactors, with major absorption peaks featuring Al–O,  $-\text{COO}^-$ ,  $-\text{CH}_3$ , and  $-\text{OH}$ .



**Figure 2.** TEM images of  $\text{AlO}_x$  nanoparticles synthesized from type A (a–c) and type B (d–f) reactors at pressures of 3.8, 5.2, and 7.5 Torr with mean sizes and standard deviations.

exhibit excellent catalytic properties because of their surface acidity and high surface area.<sup>34</sup>

In this work, we synthesized amorphous alumina nanoparticles by a nonthermal plasma approach and studied their crystallization and phase transformation behavior during postsynthetic annealing. Nonthermal plasma synthesis has shown the potential to produce a variety of nanoparticles with high purity and narrow size distributions, and the library of nanoparticle materials has been expanded from group-IV semiconductors to metal oxides and metal sulfides.<sup>35–41</sup> Furthermore, nanoparticles made by this method can be directly deposited into particle films with densities ranging from 20 to 60%.<sup>42,43</sup> The as-deposited aluminum oxide nanoparticles are annealed at 600–1100 °C for the investigation of their phase transformation behavior.

## 2. RESULTS AND DISCUSSION

### 2.1. Synthesis of Amorphous Alumina Nanoparticles.

Amorphous alumina ( $\text{AlO}_x$ ) nanoparticles were synthesized using the two reactor geometries shown in the [experimental section](#). [Figure 1a](#) shows the X-ray diffraction (XRD) spectra of as-synthesized  $\text{AlO}_x$  nanoparticle samples from both type A and B reactors at  $p = 3.8$  Torr. The absence of definitive peaks in XRD suggests that the as-synthesized  $\text{AlO}_x$  nanoparticles are

amorphous. As shown in a previous study, amorphous alumina nanoparticles have the lowest surface energy and are more thermodynamically stable compared to  $\theta$ - and  $\alpha$ -phase polymorphs at small particle sizes.<sup>46</sup>

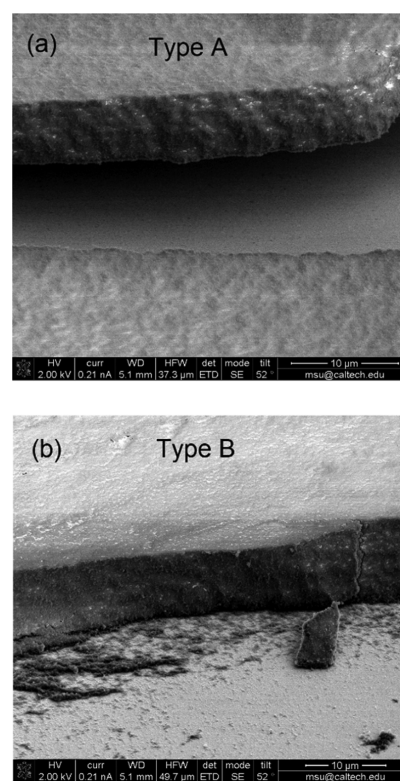
X-ray photoelectron spectroscopy (XPS) and Fourier-transform infrared spectroscopy (FTIR) measurements were performed to evaluate the surface and atomic composition of  $\text{AlO}_x$  nanoparticles from both reactor configurations ([Figure 1b,c](#)). For both samples, the main peaks in XPS correspond to O 1s, C 1s, and Al 2p at 530, 284, and 73 eV, respectively, confirming the elemental composition of  $\text{AlO}_x$  nanoparticles. Carbon incorporation (5–10 at %) is commonly observed when trimethylaluminum (TMA) is used as the aluminum source because of strong Al–C bonds.<sup>47–49</sup> The carbon content can be partly due to contamination in air, as samples are shortly exposed to air during the transfer, but can also originate from the methyl groups in TMA. Atomic percentage ratios of Al to O are around 1:3 for both A and B type reactor samples, with carbon percentages around 10–15%. The atomic ratios are in general not affected by the plasma power used for synthesis ([Figure S1](#)). High-resolution XPS spectra were analyzed to gain insight into the composition of both types of  $\text{AlO}_x$  nanoparticle samples ([Figure S2](#)). The binding energy of the Al 2p peak at  $\sim 74.6$  eV corresponds to Al–O bonding in

alumina.<sup>50,51</sup> The O 1s peak at  $\sim 531.5$  eV can be resolved into two individual peaks representing  $\text{O}^{2-}$  and  $\text{OH}^-$ .<sup>51–53</sup> FTIR spectra for samples from both reactor types reveal absorption bands related to hydroxyl ( $-\text{OH}$ ), alkyl ( $\text{C}-\text{H}$ ), ( $\text{C}-\text{O}$ ), and aluminum species ( $\text{Al}-\text{O}$  and  $\text{Al}-\text{O}-\text{Al}$ ). The peak around  $\sim 670$   $\text{cm}^{-1}$  and the shoulder located around  $\sim 860$   $\text{cm}^{-1}$  correspond to the  $\text{Al}-\text{O}$  stretching vibrations in five-fold coordinated  $\text{AlO}_5$  and four-fold coordinated  $\text{AlO}_4$ , respectively. Features from  $\text{AlO}_6$  stretching vibrations could also be present, which according to the literature lie in the  $400\text{--}650$   $\text{cm}^{-1}$  spectral range and overlap with  $\text{Al}-\text{O}$  stretching vibrations and oscillations in  $\text{AlO}_4$  and  $\text{AlO}_5$ .<sup>47,54,55</sup>

Statistics of  $\text{AlO}_x$  nanoparticle size was determined using transmission electron microscopy (TEM). At  $p = 3.8$  Torr, the average size of  $\text{AlO}_x$  nanoparticles from type A and type B reactors is  $11 \pm 3$  and  $6 \pm 1$  nm, respectively. The different particle sizes can be explained by the different plasma densities at the point of TMA injection. Nanoparticle growth in plasmas proceeds through the nucleation of clusters, many of which are initially neutral.<sup>56</sup> These clusters quickly coagulate to form nanoparticles, leading to a reduction of the overall concentration of clusters and particles. When the cluster/nanoparticle density has dropped to the level of the ion density in the plasma, there are sufficient electrons to charge most particles negatively and suppress further coagulation.<sup>56</sup> In the type B reactor, the TMA precursor is injected into a higher density plasma zone compared to the type A reactor, where the precursor is injected into a less dense plasma afterglow. Coagulation in the type B reactor is therefore suppressed at smaller particle sizes, corresponding to higher particle concentrations, compared to the type A reactor. For each type of reactor, size tuning of  $\text{AlO}_x$  nanoparticles can be achieved by varying the reactor pressure. This changes the particle residence time in the plasma and therefore tunes the time of surface growth. TEM images of as-synthesized  $\text{AlO}_x$  nanoparticles from type A and B reactors under three sets of reactor pressures are shown in Figure 2. At each pressure, the type B reactor produces smaller particles than the type A reactor. For both reactor configurations, the mean particle size increases with increasing pressure. At 3.8 and 5.2 Torr,  $\text{AlO}_x$  nanoparticles from both reactors are aggregated but nearly spherical in shape and have relatively narrow size distributions (Figure S3). At the relatively high pressure of 7.5 Torr,  $\text{AlO}_x$  nanoparticles exhibit a bimodal size distribution with both small and large irregular nanoparticles present.

We estimated the process yield of each type of reactor setup by measuring the weight of the  $\text{AlO}_x$  nanoparticle powders collected at  $p = 3.8$  Torr for 10 min. With a fixed substrate position, samples collected from both types of reactor setups were piles of white powders (Figure S4). The sample weights from the type A and B reactors were 3.2 and 7.0 mg, respectively. This corresponds to yields of 19.2 and 42.0  $\text{mg h}^{-1}$ . The current production rates are limited by the TMA and oxygen flow rates because of safety considerations.

We deposited  $\text{AlO}_x$  nanoparticle films by rastering a substrate beneath the reactor output orifice to study the optical properties of  $\text{AlO}_x$  nanoparticle films. The films were deposited with 240 raster passes and examined by scanning electron microscopy (SEM) and Mueller matrix measurements. The thicknesses of the  $\text{AlO}_x$  nanoparticle films were measured to be  $7.1 \pm 1.1$  and  $9.1 \pm 0.9$   $\mu\text{m}$  for type A and type B reactors, respectively. Characteristic cross-sectional SEM images of the nanoparticle films are shown in Figure 3.

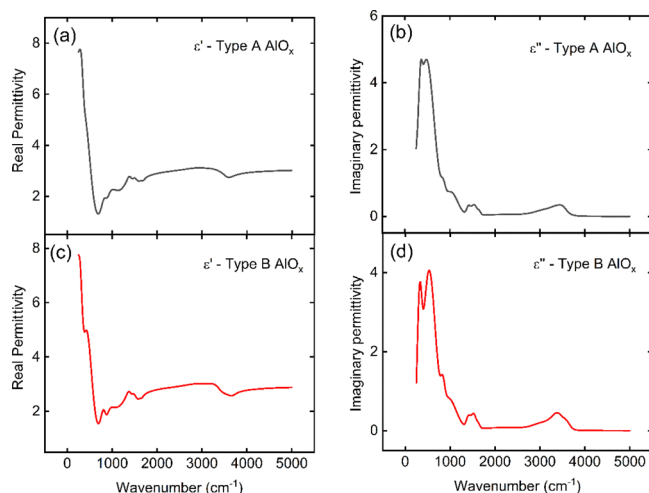


**Figure 3.** Cross-sectional SEM images of  $\text{AlO}_x$  nanoparticle laminate films synthesized from type A (a) and type B reactors (b). A correction factor of  $1/\cos(38^\circ)$  is applied in the  $y$ -axis to account for the tilt of the setup with respect to the SEM Everhart–Thornley detector.

Mueller matrix measurements, which allow for the characterization of anisotropic-depolarizing samples, including cross-polarization, were performed to extract the effective (homogenized) complex permittivity of the particle films. The measurements were also used to determine the complex permittivity of the corresponding  $\text{AlO}_x$  nanoparticles. In both type A and B films, no polarization conversion from  $p$ -polarized to  $s$ -polarized or vice versa was present. The Mueller matrix data showed only noise for elements  $\text{mm}_{13}$ ,  $\text{mm}_{31}$ ,  $\text{mm}_{22}$ ,  $\text{mm}_{23}$ ,  $\text{mm}_{32}$ ,  $\text{mm}_{41}$ , and  $\text{mm}_{42}$ . Furthermore,  $\text{mm}_{12} = \text{mm}_{21}$ . This block diagonal structure of the Mueller matrix indicates that the type A and B samples can be treated as macroscopically isotropic.<sup>57–59</sup> Therefore, the effective permittivity of each sample can be represented by a wavelength-dependent scalar. The nanoparticle films were best homogenized using the Bruggeman mixing formula. This formula has been shown to consistently produce an effective permittivity that accurately models nanoparticle films, including anisotropic-depolarizing effects.<sup>60–65</sup> Maxwell–Garnett and linear mixing formulas were also explored, but they less accurately modeled the measured data. The permittivity of the individual nanoparticles was modeled using Gaussian oscillators to represent amorphous phonon resonances while satisfying the Kramers–Kronig relations. For the type A film, a sample thickness of 7.75  $\mu\text{m}$  and a particle fill fraction of 22.3% provided the best fit to the optical interference patterns in a nearly lossless region of the amorphous alumina film between 4000 and 6250  $\text{cm}^{-1}$ . For the type B film, a thickness of 9.23  $\mu\text{m}$  and a fill fraction of 19.4% provided the best fit. Further details about Bruggeman homogenization and the correspond-



ing Gaussian oscillator model, including tables for the oscillator parameters, can be found in the [Supporting Information](#). Figure 4 shows the reconstructed imaginary part of the particle



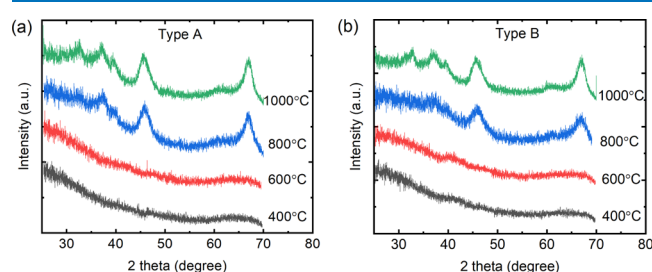
**Figure 4.** Real and imaginary parts of the complex  $\text{AlO}_x$  nanoparticle films' permittivity found in the type A reactor (a,b) and type B reactor (c,d), respectively.

permittivity. Strong oscillators in the  $300\text{--}700\text{ cm}^{-1}$  spectral range correspond to  $\text{AlO}_4$ ,  $\text{AlO}_5$ , and  $\text{AlO}_6$  stretching vibrational modes. These values corroborate our results from FTIR as well as the literature.<sup>47,54,55,63</sup> Similar to our findings from XPS and FTIR, the reconstructed permittivity shows that the particles from both types of reactors have a similar chemical composition. The depolarization constant for type A and B reactor films was  $0.261 \pm 0.005$  and  $0.407 \pm 0.006$ , respectively. This indicates predominant scattering of sphere-like inclusions post deposition. All of the above characterizations reveal that particles from type A and type B reactors have similar compositions but different sizes.

**2.2. Crystallization Behavior of Powder Samples of Amorphous Alumina Nanoparticles.** In a nonthermal plasma, crystallization of nanoparticles can occur through the heat generated by the recombination of electrons and ions on the nanoparticle surfaces.<sup>66,67</sup> Here the as-produced  $\text{AlO}_x$  nanoparticles have amorphous structures, indicating that particle heating from the nonthermal plasma is not sufficient to induce crystallization. Postsynthetic annealing of powder samples of amorphous alumina nanoparticles was explored to induce their crystallization and subsequent phase transformation to networks of crystalline alumina nanoparticles.

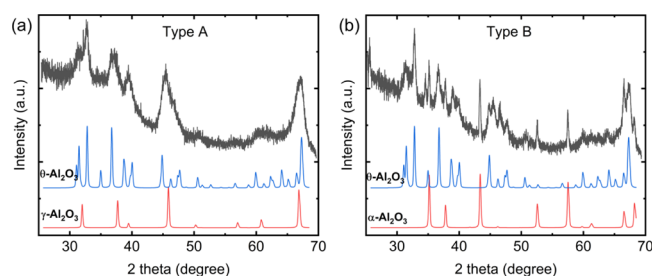
To study the crystallization and phase transformation behavior of powder samples of amorphous  $\text{AlO}_x$  nanoparticles, a pile of  $\text{AlO}_x$  nanoparticles was collected and annealed in a Thermo Scientific Lindberg Blue furnace at temperatures ranging from  $400$  to  $1100\text{ }^\circ\text{C}$  in the atmosphere. Samples collected in this manner are expected to have porosities  $>80\%$  and consist of loose agglomerates of nanoparticles.<sup>42</sup> Some of the agglomerates may have already been formed in the gas phase before deposition. The temperature ramp rate was  $\sim 50\text{ }^\circ\text{C min}^{-1}$ . Since the properties of powder samples of small  $\text{AlO}_x$  nanoparticles are of primary interest, we explored the crystallization behavior of samples synthesized at  $3.8\text{ Torr}$  from type A and B reactors. Phase transformation of amorphous alumina typically proceeds through the amorphous-to- $\gamma$  and  $\gamma$ -to- $\alpha$  phase transitions<sup>68,69</sup> or with an additional transition to

the  $\theta$ -phase between the transformation from the  $\gamma$ - to  $\alpha$ -phase,<sup>70</sup> before reaching the thermodynamically stable  $\alpha$ -phase. Our observations reveal that powder samples of  $\text{AlO}_x$  nanoparticles from both types of reactors begin to crystallize at  $800\text{ }^\circ\text{C}$  producing a mixture of  $\theta$ - and  $\gamma$ -phases, as shown in Figure 5a,b. The crystallization temperature is consistent with that from the literature.<sup>9,46</sup>



**Figure 5.** XRD patterns of the postsynthesis annealed  $\text{AlO}_x$  nanoparticles from (a) type A and (b) type B reactors, with annealing temperatures ranging from  $400$  to  $1000\text{ }^\circ\text{C}$  and an annealing time of  $18\text{ h}$ .

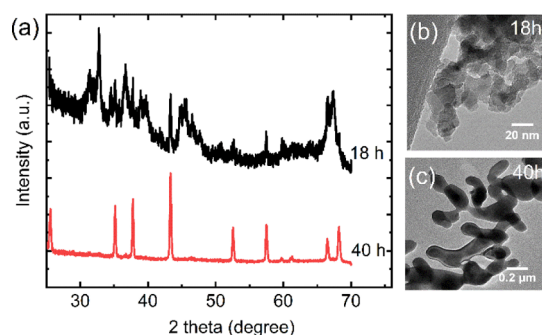
As the annealing temperature increased up to  $1100\text{ }^\circ\text{C}$ , we observed that the powder samples of  $\text{AlO}_x$  nanoparticles from the type A and B reactors form different crystalline phases (Figure 6). The samples of larger  $\text{AlO}_x$  nanoparticles from the



**Figure 6.** XRD patterns of the postheated  $\text{AlO}_x$  nanoparticles from (a) type A and (b) type B. Both samples were annealed at  $1100\text{ }^\circ\text{C}$  for  $18\text{ h}$ . The bottom columns in both graphs show the reference profiles of  $\gamma$ -,  $\theta$ -, and  $\alpha$ -phase aluminum oxides.

type A reactor form a mixture of  $\theta$ - and  $\gamma$ -phases at  $1100\text{ }^\circ\text{C}$ , whereas the samples of smaller  $\text{AlO}_x$  nanoparticles from the type B reactor form a mixture of  $\theta$ - and  $\alpha$ -phases. Time of postsynthetic annealing also affects phase transformation of the type B reactor  $\text{AlO}_x$  nanoparticle powders. When the annealing time increased up to  $40\text{ h}$ , type B  $\text{AlO}_x$  nanoparticle powders form particle networks of phase pure  $\alpha\text{-Al}_2\text{O}_3$  nanocrystals (Figure 7).

This transformation is also accompanied by a significant crystal growth. The mean crystallite sizes of crystalline alumina particles after  $18\text{ h}$  annealing were estimated using Scherrer fittings. Annealing for  $18\text{ h}$  of  $\sim 6\text{ nm}$   $\text{AlO}_x$  nanoparticle powders at  $1100\text{ }^\circ\text{C}$  resulted in a particle network consisting of a mixture of  $\sim 30\text{ nm}$   $\theta\text{-Al}_2\text{O}_3$  and  $>100\text{ nm}$   $\alpha\text{-Al}_2\text{O}_3$  particles (Figure S5). Samples of phase-pure  $\alpha\text{-Al}_2\text{O}_3$  particles obtained after  $40\text{ h}$  are also estimated to be comprised of nanocrystals larger than  $100\text{ nm}$ . The crystalline grain sizes are confirmed by TEM images (Figure 7b,c). It is interesting to observe that the powders of larger  $\text{AlO}_x$  nanoparticles from the type A reactor never exhibit  $\alpha\text{-Al}_2\text{O}_3$  phase even with longer annealing times.



**Figure 7.** (a) XRD pattern of type B  $\text{AlO}_x$  nanoparticles heated at 1100 °C for 18 and 40 h; TEM images of (b)  $\text{AlO}_x$  nanoparticles annealed at 1100 °C for 18 h and (c)  $\text{AlO}_x$  nanoparticles annealed at 1100 °C for 40 h.

As the powder samples of  $\text{AlO}_x$  nanoparticles from both types of reactors have a similar composition, we postulated that the difference in their phase transformation behavior is likely due to the different sizes of their as-synthesized constituent particles. To test this assumption, we investigated the phase transformation behavior of powder samples of the large  $\text{AlO}_x$  particles with mean sizes around 11 and 15 nm synthesized in the type B reactor with higher reactor pressures. XRD patterns taken after 18 h of annealing time reveal that powders of smaller  $\sim 6$  nm  $\text{AlO}_x$  nanoparticles form  $\alpha$ -phase  $\text{Al}_2\text{O}_3$  along with  $\theta$ - $\text{Al}_2\text{O}_3$ , while powders of larger  $\sim 11$  and  $\sim 15$  nm  $\text{AlO}_x$  nanoparticles only form  $\theta$ - $\text{Al}_2\text{O}_3$  and do not exhibit any  $\alpha$ -phase features (Figure S6). These observations support our assumption that powders of initially smaller size  $\text{AlO}_x$  nanoparticles have a higher tendency to transform to the  $\alpha$ -phase after annealing.

It has been pointed out that necking and densification of particles start to occur when annealing amorphous  $\text{AlO}_x$  nanoparticles, forming nanoporous structures before crystallization.<sup>46,71,72</sup> It is likely that during the annealing, the rate of densification and neck formation is faster in powder samples of smaller particles compared to larger particles as the neck growth is dominated by mass transport and is thus enhanced in smaller size particles.<sup>73</sup> The fact that powder densification can be promoted by a decrease of particle sizes has also been observed in other nanoparticle systems.<sup>74</sup> After neck growth, the interconnected structures tend to transform to  $\alpha$ -phase  $\text{Al}_2\text{O}_3$  as the temperature further increases because it is the thermodynamically stable phase for bulk  $\text{Al}_2\text{O}_3$ .

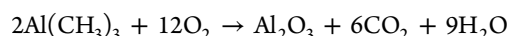
### 3. CONCLUSIONS

Amorphous alumina nanoparticles with average sizes ranging from 6 to 22 nm were successfully synthesized using a nonthermal plasma approach with two different reactor geometries with typical yields of 19 and 42 mg h<sup>-1</sup>, respectively. Infrared Mueller matrix measurements indicated that the optical properties of the nanoparticle film could be modeled by a homogenized effective refractive index. The homogenized refractive index of the particle film was shown to be accurately represented using the Bruggeman effective medium model. Based on this model, particle fill fractions were estimated to be around 20% for both type A and type B reactors. Furthermore, the refractive index of the amorphous alumina nanoparticles was modeled using Gaussian oscillators, showing clear  $\text{AlO}_4$ ,  $\text{AlO}_5$ ,  $\text{AlO}_6$ , and Al–OH spectral peaks, matching reports in the literature. Post-thermal annealing of

powder samples of  $\text{AlO}_x$  particles from both types of reactors led to crystallization, forming a mixture of  $\theta$ - and  $\gamma$ -phases at 800 °C, while powder samples of small  $\text{AlO}_x$  nanoparticles with average diameters of  $\sim 6$  nm were transformed into phase-pure  $\alpha$ - $\text{Al}_2\text{O}_3$  upon annealing at 1100 °C. Powder samples of larger  $\text{AlO}_x$  nanoparticles never formed  $\alpha$ - $\text{Al}_2\text{O}_3$ .

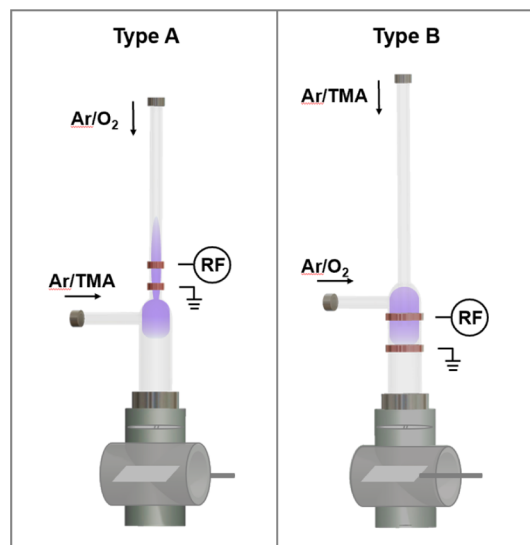
## 4. EXPERIMENTAL SECTION

**4.1. Nanoparticle Synthesis.** For the synthesis of amorphous alumina ( $\text{AlO}_x$ ) nanoparticles via nonthermal plasma, TMA and oxygen ( $\text{O}_2$ ) gas were used as precursors, with argon as the carrier gas. In the plasma region, TMA is decomposed via electron impact or radical abstraction reactions, forming reactive metal atoms or partially decomposed TMA fragments. The reactive species can subsequently react with oxygen atoms to form  $\text{Al}_2\text{O}_3$ .<sup>44</sup> We considered the following chemical equation to control appropriate flow rates



Based on the stoichiometric molar ratio of TMA and oxygen ( $\text{TMA}/\text{O}_2 = 1:6$ ), over 6 times more oxygen than TMA should be fed for complete oxidation of TMA to  $\text{Al}_2\text{O}_3$  and other reaction products ( $\text{CO}_2$  and  $\text{H}_2\text{O}$ ). We chose an excess oxygen flow rate of 6 standard cubic centimeters per minute (sccm) compared with a TMA flow rate of 0.2 sccm.

A schematic of the two types of reactors used in this work is shown in Figure 8.  $\text{AlO}_x$  nanoparticles were synthesized in a



**Figure 8.** Schematic of the two types of nonthermal plasma reactors used for  $\text{AlO}_x$  nanoparticle synthesis and film deposition.

nonthermal, low pressure, flow-through reactor equipped with a 13.56 MHz radio frequency (RF) capacitively coupled plasma source similar to that used in refs 37 and 38. Because two precursors can spontaneously react with each other to produce uncontrolled products,<sup>45</sup> we injected both precursor species separately into the plasma for dissociation to occur in the plasma zone. There are two strategies that have been demonstrated before for the successful synthesis of metal oxide nanoparticles.<sup>37,38</sup> In the first method, denoted as type A,  $\text{O}_2$  diluted in Ar gas was injected from the top inlet of the reactor and flowed through the region where RF power was applied. Meanwhile, 0.2 sccm of TMA vapor with 6 sccm of Ar gas was

injected from a sidearm tube into the downstream region of the Ar/O<sub>2</sub> plasma. In this afterglow zone, AlO<sub>x</sub> nanoparticles nucleated and grew. In the second method, denoted as type B, the TMA vapor diluted in Ar was injected through an inlet tube that extended into the main reactor chamber, while O<sub>2</sub> gas diluted with Ar gas was passed through a sidearm tube and into the space around the upper injection tube. The ring electrodes were placed such that the plasma initiated about 1 cm above the end of the top injection tube and the discharge extended downstream of the tube end in order to dissociate TMA and O<sub>2</sub> precursors individually before they mix in the main reactor chamber. The as-synthesized AlO<sub>x</sub> nanoparticles in both configurations were collected on silicon wafers through a slit-shaped orifice where supersonic nanoparticle impaction produced a curtain of nanoparticles traveling at high speeds.<sup>42</sup> For each type of reactor, three pressure conditions were studied by using three different orifice sizes (0.3, 0.4, 0.5 mm × 8 mm) while keeping the gas flow rates constant.

For optical characterization, nanoparticle films were deposited by using the 0.5 mm × 8 mm orifice and passing a piece of Si wafer carrying a 300 nm Au film below the orifice with 240 raster passes. The gas flow rates and upstream and downstream pressures are summarized in Table 1.

**Table 1. Summary of Synthesis Parameters Used in This Study**

	gas	flow rate [sccm]	$P_{\text{up}}$ [Torr]	$P_{\text{down}}$ [Torr]
type A	O <sub>2</sub> diluted in Ar (O <sub>2</sub> /Ar)	6(O <sub>2</sub> )/60(Ar)	3.8	0.42
	TMA vapor with Ar (TMA/Ar)	0.2(TMA)/6(Ar)		
type B	O <sub>2</sub> diluted in Ar (O <sub>2</sub> /Ar)	6(O <sub>2</sub> )/60(Ar)	3.8	0.47
	TMA vapor with Ar (TMA/Ar)	0.2(TMA)/6(Ar)		

**4.2. Characterization.** XRD was performed with a Bruker D8 Discover 2D X-ray diffractometer equipped with a Co K $\alpha$  radiation point source. Instrument broadening was obtained by measuring a standard LaB<sub>6</sub> crystal powder sample with the same scanning parameters (Figure S7). For XRD analysis, aluminum oxide nanoparticles were directly deposited onto Si wafers to form a pile of powder. The XRD patterns were converted to the wavelength of a Cu source ( $\lambda = 1.54 \text{ \AA}$ ) for data analysis.

TEM images were taken from a Tecnai T12 microscope with an accelerating voltage of 120 kV. Nanoparticles were either directly deposited from the gas phase or drop-cast in a methanol dispersion on holey carbon TEM grids for imaging.

FTIR was performed with a Bruker ALPHA FTIR spectrometer using the attenuated total reflection (ATR) module in a nitrogen-filled glovebox. AlO<sub>x</sub> nanoparticles were dispersed in methanol and drop-cast onto the ATR crystal. Nanoparticles were allowed to dry before taking measurements.

XPS was performed with a PHI Versa Probe III XPS and UPS system. For XPS analysis, aluminum oxide nanoparticles were deposited onto Si wafers with 30 raster passes to form a film.

Nanoparticle laminate film thicknesses were measured empirically by cross-sectioning the nanoparticle laminate films with a Ga focused ion beam and imaging with a scanning

electron microscope (FEI Nova 600 NanoLab DualBeam) at a 52° tilt. The cross-sectioning was performed in two steps: a regular cross-section (30 kV, 1 nA) approximately 2  $\mu\text{m}$  in width was cut first followed by a cleaning cross-section (30 kV, 30 pA). The thickness of the cross-sections was measured with ImageJ with a correction factor of  $1/\cos(38^\circ)$  in the  $y$ -axis to account for the tilt.

To analyze the film optical properties, the first four columns of the angle- and wavelength-resolved Mueller matrix were measured in the reflection mode. Mueller matrix measurements were performed using an IR-VASE Mark II ellipsometer with an AutoRetarder from the J.A. Woollam Company. The configuration was polarizer–sample–compensator–analyzer. The measurement spectral range extended from 250 to 5000  $\text{cm}^{-1}$  with a resolution of 7.7  $\text{cm}^{-1}$ . The angular range was 40 to 70° from the surface normal, with an angular resolution of 5°. Data was averaged over 400 measurements—5 days of continuous measurement per sample under ambient conditions. Once the samples were measured, an oscillator model of the film permittivity was constructed using the software WVASE32 from J.A. Woollam. Model parameters such as the film thickness and particle fill fraction were initialized based on the empirical measurement averages and constrained by 3 times the measurement standard deviations. Initial values for the particle oscillator model were taken from the literature. All model parameters were simultaneously fitted using the full angle and wavelength-resolved Mueller matrix data.

## ■ ASSOCIATED CONTENT

### Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acsomega.0c03353>.

Atomic concentration in samples from type B reactor obtained by XPS with power varying from 5 W to 40 W; XPS high resolution spectra of Al 2p peak, O 1s peak, and C 1s peak; size distributions corresponding to the TEM images; photograph showing AlO<sub>x</sub> nanoparticles deposited from type A and type B reactors for same period of time; Scherrer fittings of XRD patterns; XRD patterns of samples from type B reactor for three nanoparticle sizes; and Gaussian oscillator parameters used to reconstruct the permittivity of nanoparticles from type A and type B reactors (PDF)

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## Notes

The authors declare no competing financial interest.

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